Solving Equations With Square Roots

Quick Review: To solve an equation that has a square root, get the radical by itself and square both sides. This may create a false solution so you must check your answer.

Example: Solve $x - 6 = \sqrt{x}$

solution: Square both sides to get $x^2 - 12x + 36 = x$ or $x^2 - 13x + 36 = 0$ which factors into (x-9)(x-4) = 0. This gives the answers x = 9 and x = 4. However, x = 4 does not check, so the only correct solution is x = 9.

Problems

Solve each equation for all values of the unknown. Some equations may not have any solution.

1.
$$\sqrt{x+1} = x-1$$

2.
$$\sqrt{4-x} = x+8$$

3.
$$2-x=2\sqrt{2-x}$$

4.
$$\sqrt{1+2x} = x-1$$

5.
$$x+4=3\sqrt{2x-1}$$

6.
$$\sqrt{x^2 - 5x} = 2 - x$$